

Measurement of charm and beauty dijet cross sections in photoproduction at HERA using the H1 vertex detector

The H1 Collaboration

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Abstract. A measurement of charm and beauty dijet photoproduction cross sections at the ep collider HERA is presented. Events are selected with two or more jets of transverse momentum $p_t^{\text{j}et_{1(2)}} > 11(8)$ GeV in the central range of pseudo-rapidity $-0.9 < \eta^{\text{j}et_{1(2)}} < 1.3$. The fractions of events containing charm and beauty quarks are determined using a method based on the impact parameter, in the transverse plane, of tracks to the primary vertex, as measured by the H1 central vertex detector. Differential dijet cross sections for charm and beauty, and their relative contributions to the flavour inclusive dijet photoproduction cross section, are measured as a function of the transverse momentum of the leading jet, the average pseudo-rapidity of the two jets and the observable x_γ^{obs} . Taking into account the theoretical uncertainties, the charm cross sections are consistent with a QCD calculation in next-to-leading order, while the predicted cross sections for beauty production are somewhat lower than the measurement.

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1 Introduction

A measurement is presented of charm and beauty production in ep collisions at HERA using events with two or more jets at high transverse momentum. The measurement is carried out in the photoproduction region in which a quasi-real photon, with virtuality $Q^2 \sim 0$, is emitted from the incoming positron and interacts with a parton from the proton. Differential charm and beauty dijet cross sections are measured and compared to calculations in perturbative quantum chromodynamics (pQCD) performed to next-to-leading order (NLO).

In pQCD calculations, the photoproduction of charm and beauty proceeds dominantly via the direct photon–gluon fusion process $\gamma g \rightarrow c\bar{c}$ or $b\bar{b}$, where the photon interacts with a gluon from the proton to produce a pair of heavy quarks in the final state. Previous charm measurements have confirmed this prediction [1–4]. In leading order QCD models a successful description of the data is obtained when additional contributions from processes involving resolved photons are taken into account [2, 3]. In such resolved photon processes the quasi-real photon fluctuates into a hadronic state before the hard interaction and thus acts as a source of partons. In the massless scheme, a large fraction of these resolved photon processes is due to heavy quark excitation, in which one of the partons that enters the hard interaction is a heavy quark (c or b) originating from the resolved photon or the proton.

In this analysis events containing heavy quarks are distinguished from light quark events by the long lifetimes of c and b flavoured hadrons, which lead to displacements of tracks from the primary vertex. This technique, based on the precise spatial information from the H1 silicon vertex detector, was introduced in recent H1 measurements of the charm and beauty structure functions $F_2^{c\bar{c}}$ and $F_2^{b\bar{b}}$ in deep inelastic scattering [5, 6], and is now applied to dijet events in photoproduction. This analysis provides the first simultaneous measurement of charm and beauty in photoproduction, extending to larger values of transverse jet momentum than previous measurements [1–4, 7–10]. The regions of small transverse momentum and large pseudo-rapidities are excluded from the measurement, due to trigger requirements and the limited angular acceptance of the vertex detector.

The differential charm and beauty dijet cross sections are measured as functions of the transverse momentum of the leading jet $p_t^{\text{jet}1}$, of the mean pseudo-rapidity $\bar{\eta}$ of the two jets, and of the variable x_γ^{obs} which, in a leading order picture, corresponds to the fraction of the photon’s energy in the proton rest frame that enters the hard interaction. For direct photon–gluon fusion processes $x_\gamma^{\text{obs}} \sim 1$, while for resolved photon processes x_γ^{obs} can be small. The

measured differential charm and beauty cross sections, together with the measured flavour inclusive cross sections, are used to determine the relative contribution from charm and beauty events to dijet photoproduction. The results are compared with calculations in perturbative quantum chromodynamics at next-to-leading order and with predictions from Monte Carlo simulations in which leading order matrix elements are implemented, and contributions from higher orders are approximated using parton showers.

This paper is structured as follows. In Sect. 2 the experimental apparatus is briefly described. Event and track selections are detailed in Sect. 3. The method to determine the contributions of charm and beauty events is outlined in Sect. 4. Theoretical calculations performed in the framework of perturbative QCD are discussed in Sect. 5. The cross section measurements and their systematic uncertainties are presented in Sect. 6. Properties of a heavy quark enriched data sample are investigated in Sect. 7. A summary of the results is given in Sect. 8.

2 H1 detector

The H1 detector is described in detail in [11]. Charged particles emerging from the ep interaction region are measured by the central tracking detector (CTD) in the pseudo-rapidity range $-1.74 < \eta < 1.74^1$. The CTD consists of two large cylindrical central jet drift chambers (CJCs), two z chambers and two multi-wire proportional chambers arranged concentrically around the beam-line in a magnetic field of 1.15 T. The CTD provides triggering information based on track segments from the CJC in the r – ϕ plane, transverse to the beam direction, and on the z position of the vertex from the multi-wire proportional chambers. The CJC tracks are linked with hits in the Central Silicon Tracking detector (CST) [12], which consists of two cylindrical layers of silicon strip sensors, surrounding the beam pipe at radii of 57.5 mm and 97 mm from the beam axis, covering an angular range of $30^\circ < \theta < 150^\circ$ for tracks passing through both layers. The detector provides hit resolutions of $12 \mu\text{m}$ in r – ϕ with an average efficiency of 97%.

For CTD tracks with CST hits in both layers the impact parameter δ , i.e. the transverse distance of closest approach to the nominal vertex, can be measured with a resolution of $\sigma_\delta \approx 33 \mu\text{m} \oplus 90 \mu\text{m}/p_t$ [GeV]. The first term represents the intrinsic resolution and includes the uncertainty of the CST alignment, the second term corresponds to the contribution from multiple scattering in the beam pipe and the CST, which depends on the transverse momentum p_t of the track.

Charged and neutral particles are measured in the liquid argon (LAr) calorimeter which surrounds the tracking chambers and covers the range $-1.5 < \eta < 3.4$ and a lead-scintillating fibre calorimeter SpaCal, covering the backward region $(-4.0 < \eta < -1.4)$ [13]. The measurements

¹ The pseudo-rapidity is given by $\eta = -\ln \tan(\theta/2)$, where θ is measured with respect to the z -axis given by the proton beam direction.

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from the CTD and the calorimeters are combined to reconstruct the final state particles [14]. The luminosity determination is based on the measurement of the Bethe-Heitler process ($ep \rightarrow ep\gamma$), where the photon is detected in a calorimeter located downstream of the interaction point in the positron beam direction.

3 Event and track selection

The data sample corresponds to an integrated luminosity of 56.8 pb^{-1} and was recorded with the H1 experiment during the years 1999 and 2000. During this time HERA was operated with positrons of 27.5 GeV and protons of 920 GeV. The events were triggered by a combination of signals from the calorimeters, the central drift chambers and the multi-wire proportional chambers. Photoproduction events are selected by requiring that there be no isolated high energy electromagnetic cluster detected

in the calorimeters consistent with a signal from the scattered positron. This restricts the range of negative four-momentum transfer squared to $Q^2 < 1 \text{ GeV}^2$. The inelasticity y is calculated using the hadronic final state [15], and the measurement is restricted to the range $0.15 < y < 0.8$. The jets are reconstructed from the final state particles using the inclusive k_t algorithm [16] in the p_t recombination scheme [17], with distance parameter $R = 1$ in the η - ϕ plane. The event selection requires at least two jets in the central pseudo-rapidity range $-0.9 < \eta < 1.3$ with transverse energy $p_t^{\text{jet}(1,2)} > 11$ (8) GeV.

CTD tracks are selected which are linked to hits in both r - ϕ layers of the CST. These tracks are required to have a transverse momentum above 500 MeV and a polar angle in the range $30^\circ < \theta_{\text{track}} < 150^\circ$. Events are selected which contain at least one selected track associated to one of the two leading jets. The final sample consists of 80 769 events.

To correct for detector effects, such as detector resolutions and inefficiencies, large samples of charm, beauty

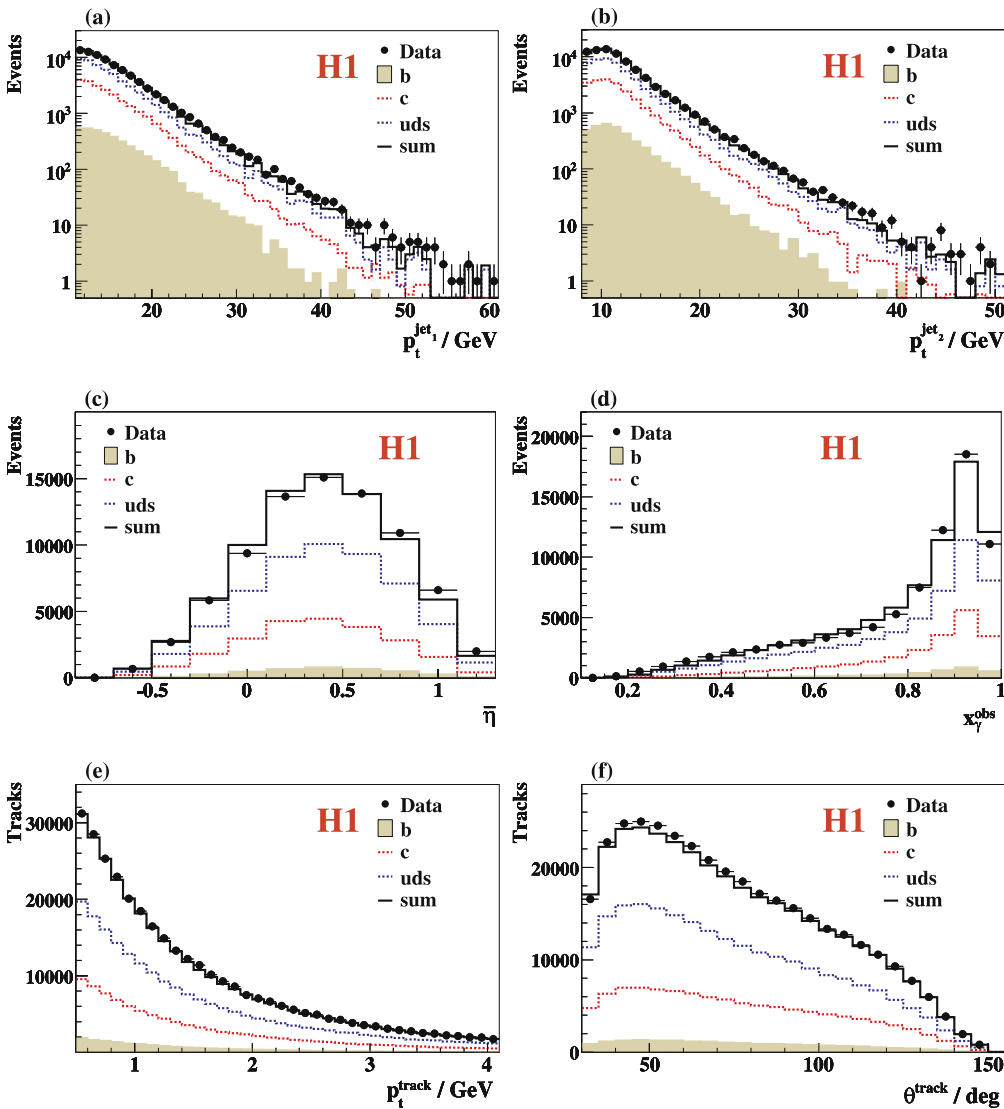


Fig. 1. Distributions of **a** the transverse momentum $p_t^{\text{jet}1}$ of the leading jet, **b** the transverse momentum $p_t^{\text{jet}2}$ of the second jet, **c** the mean pseudo-rapidity $\bar{\eta}$ of the two jets, **d** the observable x_γ^{obs} , **e** the transverse momentum of the selected tracks and **f** the polar angle of the selected tracks. The expectation from the PYTHIA Monte Carlo simulation is included in the figure, showing the contributions from the various quark flavours after applying the scale factors obtained from the fit to the subtracted significance distributions of the data (see Sect. 4)

and light quark events are generated using the Monte Carlo program PYTHIA [18] (for details see Sect. 5). All samples are passed through a detailed simulation of the H1 detector response based on the GEANT program [19] and the same reconstruction and analysis algorithms as used for the data.

Figure 1 shows the distributions of the transverse momentum of the leading jet $p_t^{\text{jet}1}$, and of the jet with the second highest transverse momentum $p_t^{\text{jet}2}$ (Fig. 1a and b), of the mean pseudo-rapidity $\bar{\eta} = (\eta^{\text{jet}1} + \eta^{\text{jet}2})/2$ of the two jets (Fig. 1c) and of x_γ^{obs} (Fig. 1d). The observable x_γ^{obs} is defined as $((E - p_z)_{\text{jet}1} + (E - p_z)_{\text{jet}2}) / \sum (E - p_z)$ where the sum runs over all measured particles of the final state. In Fig. 1e and f the transverse momentum and polar angular distributions of the selected tracks are shown. The simulation based on the PYTHIA event generator provides a good description of all distributions, after scaling the contributions from light quark, charm and beauty events. The scale factors are obtained from fits to the signed impact parameter distributions, as described below in Sect. 4.

4 Quark flavour separation

The fractions of events containing charm and beauty quarks are determined using the same method as in a previous measurement [5], based on the impact parameter of selected tracks which is given by the transverse distance of closest approach to the reconstructed event vertex. The signed impact parameter δ is defined as positive if the angle between the axis of the associated jet and the line joining the primary vertex to the point of closest approach of the track is less than 90° , and is defined as negative otherwise.

The distribution of δ is shown in Fig. 2a. The data are well described by the simulation. Due to the long lifetimes of charm and beauty flavoured hadrons the δ distribution is asymmetric, the number of tracks with positive values exceeding the number of tracks with negative values. While the component that arises from light quarks is almost symmetric, the c component has a moderate asymmetry and the b component shows a marked asymmetry. The asymmetry seen at $|\delta| > 0.1$ cm is mainly due to decays of long lived strange particles such as K_S^0 . In order to reduce the

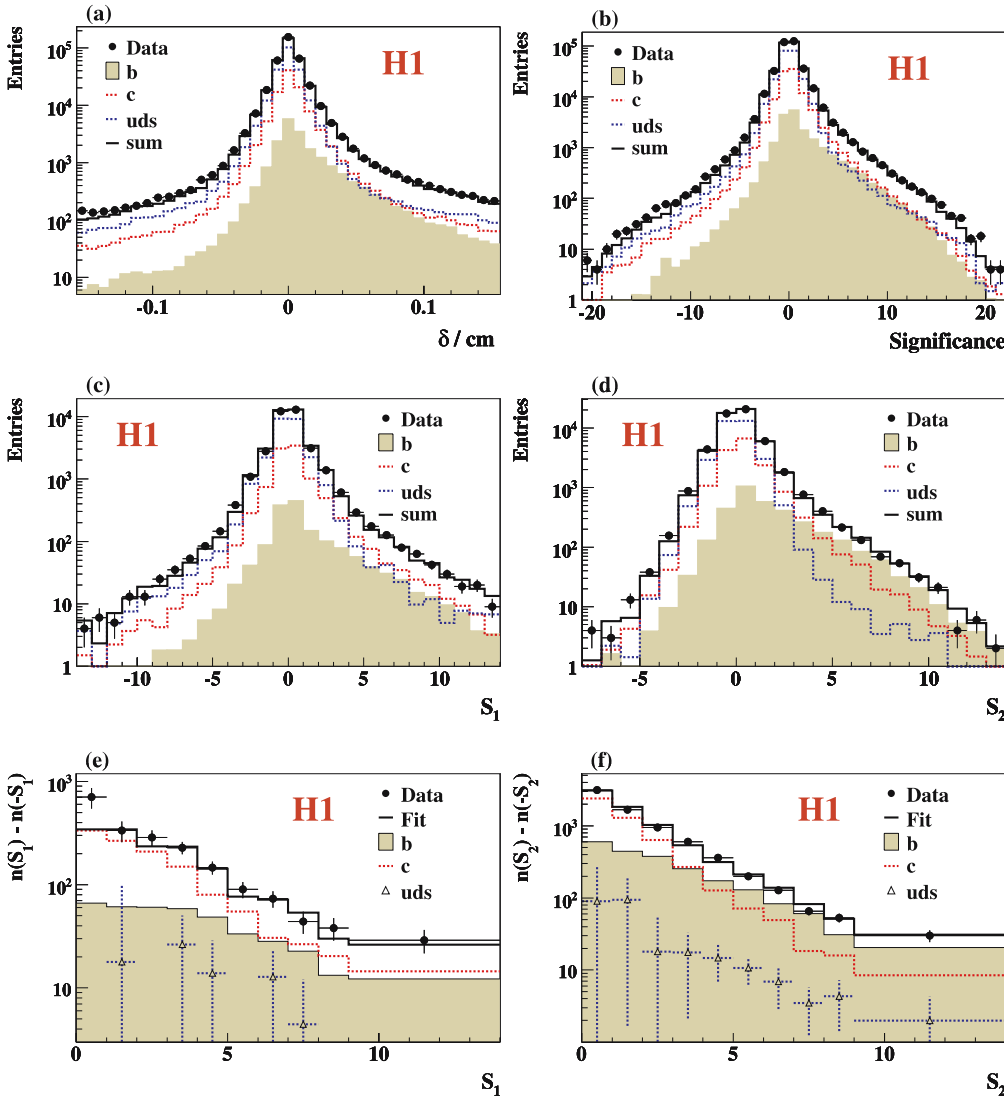


Fig. 2. Distributions of **a** the signed impact parameter δ of selected tracks, **b** the signed significance, **c** the significance S_1 of tracks in jets with exactly one selected track, **d** the significance S_2 of the track with the second highest significance in jets with two or more selected tracks, **e** the subtracted signed significance for the sample with exactly one selected track, **f** the subtracted signed significance for the sample with two or more selected tracks. In **b** to **f** only tracks with an impact parameter $|\delta| < 0.1$ cm are considered. The expectation from the PYTHIA Monte Carlo simulation is included in the figure, showing the contributions from the various quark flavours after applying the scale factors obtained from the fit to the subtracted significance distributions of the data (see Sect. 4)

effects of the strange component, tracks with $|\delta| > 0.1$ cm are rejected. The significance, defined as the ratio of the impact parameter δ to its error, is shown in Fig. 2b for all selected tracks with $|\delta| < 0.1$ cm.

The distributions of S_1 (Fig. 2c) and of S_2 (Fig. 2d) show the significance of the selected track in jets with exactly one selected track associated to the jet (S_1) and the significance of the track with the second highest absolute significance in jets with two or more selected tracks (S_2). For jets contributing to the distribution of S_2 it is required that the tracks with the first and second highest absolute significance in the jet have the same sign of δ . At moderate and large values of S_2 the beauty contribution exceeds that from charm.

In order to substantially reduce the uncertainty due to the resolution of δ and the light quark normalisation the negative bins in the S_1 and S_2 distributions are subtracted from the positive bins. These subtracted S_1 and S_2 distributions are shown in Fig. 2e and f. The distributions are dominated by charm quark events, with an increasing fraction of beauty quark events towards larger values of significance. The contribution from light quarks is seen to be small.

The c , b and light quark fractions in the data are extracted using a simultaneous least squares fit of simulated reference distributions for c , b and light quark events, obtained from the PYTHIA Monte Carlo simulation, to the measured subtracted S_1 and S_2 distributions (Fig. 2e and f). The total number of events before any CST track selection is also used in the fit. The Monte Carlo contributions from charm, beauty and light quark events are scaled by factors P_c , P_b and P_l respectively, which are the free parameters of the fit. Only the statistical errors of the data and the Monte Carlo simulation are taken into account. The fit to the complete data sample gives scale factors $P_c = 1.45 \pm 0.14$, $P_b = 1.98 \pm 0.22$, and $P_l = 1.44 \pm 0.05$ and has a $\chi^2/n.d.f.$ of 13.1/18. The Monte Carlo distributions shown in Figs. 1, 2, 6 and 7 are scaled by these factors. Consistent results are found when alternative methods are used to separate the quark flavours, such as the explicit reconstruction of secondary vertices described in Sect. 7.

5 Calculations in perturbative QCD

The Monte Carlo simulation programs PYTHIA [18] and CASCADE [20] provide cross section predictions in pQCD at leading order. Parton showers are implemented to account for higher order effects. PYTHIA uses the DGLAP parton evolution equations [21] while CASCADE contains an implementation of the CCFM evolution equations [22].

PYTHIA is run in an inclusive mode (MSTP(14) = 30 [18]) in which direct and resolved photon processes, including heavy quark excitation, are generated using massless matrix elements for all quark flavours. The CTEQ5L [23] parton densities are used for the proton and those of SaS1D [24] for the photon. The charm and beauty quark masses are set to 1.5 and 4.75 GeV respectively, and the fragmentation is modelled by the Lund string

model [25], using the Peterson function [26] for the longitudinal fragmentation of beauty and charm quarks.

Additional Monte Carlo samples of charm, beauty and light quark events are generated using the Monte Carlo generator CASCADE with the charm and beauty masses as used in PYTHIA. The process $\gamma g \rightarrow c\bar{c}$ or $b\bar{b}$ is implemented using off-shell matrix elements convoluted with k_t unintegrated parton distributions in the proton. In this analysis the parametrisation A0 [27] is used for the parton distributions.

QCD calculations to next-to-leading order are performed using the program FMNR [28]. FMNR implements the calculation at fixed order in the massive scheme, i.e. charm and beauty quarks are generated dynamically in the hard process via boson–gluon fusion diagrams and the parton distributions for the proton and the photon consist only of light quarks (uds) and gluons. FMNR provides weighted parton level events with two or three outgoing partons, i.e. the heavy quark antiquark pair and possibly a third parton. Values of 1.5 and 4.75 GeV are chosen for the c and b quark masses respectively. The renormalisation and factorisation scales are set to the transverse masses $m_t = \sqrt{m_q^2 + p_{t,q\bar{q}}^2}$, where $p_{t,q\bar{q}}^2$ is the average of the squared transverse momenta of the heavy quark and anti-quark. The CTEQ5F3 parameterisation [23] is used for the parton distribution functions in the proton. Contributions from processes with resolved photons are calculated using the GRV-G HO distributions of partons in the photon [29]. In the next-to-leading order prediction these contributions are found to be small ($\sim 3\%$).

In order to compare the parton level calculation with the data, corrections from parton to hadron level are applied which are determined using the PYTHIA Monte Carlo event generator. The jets at both the parton and the hadron level are reconstructed using the inclusive k_t jet-algorithm in the p_t recombination scheme. The bin-by-bin corrections from parton to hadron level are found to be less than $\pm 10\%$ everywhere except in the bins $0.7 < x_\gamma^{\text{obs}} < 0.85$ and $0.85 < x_\gamma^{\text{obs}} < 1$ where the corrections are about $+35\%$ and -15% respectively.

Theoretical uncertainties of the NLO calculation are estimated by independent variations of the renormalisation and factorisation scales by factors of one half and two, and the maximal changes to the cross section predictions of 30%–35% for charm and 20%–30% for beauty are taken as systematic errors. The c (b) masses are varied between 1.4 and 1.6 (4.5 and 5) GeV leading to cross section changes of up to $\pm 4\%$. The cross section variations when using other proton structure functions such as CTEQ6M [30], MRSG or MRST1 [31] are less than 8% in all regions of the measurement. The latter uncertainty is added in quadrature to the uncertainties from the scales and the quark mass.

6 Cross section measurement

For the measurement of the charm and beauty cross sections, the scale factors P_c and P_b , which are determined from fits of the subtracted significance distributions to the

data, are multiplied with the cross section predictions of the PYTHIA Monte Carlo simulation. For the measurement of the differential charm and beauty cross sections the fit is performed separately in each bin i . The resulting scale factors $P_{c,i}$ and $P_{b,i}$ are then multiplied with the bin-averaged cross section predictions of the PYTHIA Monte Carlo simulation, divided by the respective bin size. In addition, the measured differential cross sections for charm and beauty dijet production are divided by the corresponding flavour inclusive cross sections to obtain the fractional contributions of events containing charm and beauty quarks. The flavour inclusive dijet cross section is measured by correcting the observed number of events before track selections for detector efficiencies and acceptances and dividing by the integrated luminosity.

6.1 Systematic uncertainties

Systematic uncertainties of the cross section measurement are evaluated by variations applied to the Monte Carlo simulations. The resulting systematic uncertainties of the total charm and beauty dijet cross sections are listed in Table 1 and detailed below.

- An uncertainty in the δ resolution of the tracks is estimated by varying the resolution by an amount that encompasses the differences between the data and simulation (Fig. 2). This is achieved by applying an additional Gaussian smearing in the Monte Carlo simulation of $200\ \mu\text{m}$ to 5% of randomly selected tracks and of $25\ \mu\text{m}$ to the rest.
- The uncertainty of the jet axis reconstruction is estimated by shifting the jet axis in azimuth ϕ by $\pm 1^\circ$.
- The reconstruction efficiency of central drift chamber tracks is uncertain to the level of 2% and the efficiency for these tracks to have hits in both r - ϕ layers of the silicon vertex detector is known to 1%.
- The uncertainty resulting from the shape of the subtracted significance distributions S_1 and S_2 for light quarks (Fig. 2e and f) is estimated by repeating the fits with the light quark S_1 and S_2 distributions varied by $\pm 50\%$ of the default value.
- The systematic error arising from the uncertainty of the underlying physics model is estimated by varying the contribution from resolved photon processes in the PYTHIA prediction by $\pm 50\%$, and by reweighting the p_t distribution as predicted by PYTHIA to that of CASCADE. These variations lead to changes of the cross sections of $\pm 7\%$ for charm and $\pm 14\%$ for beauty.
- The uncertainties in the description of the heavy quark fragmentation are estimated by repeating the fits with a Monte Carlo simulation in which the Lund Bowler function [25] is used for the longitudinal fragmentation instead of the Peterson function.
- The uncertainties arising from the various D and B hadron lifetimes, fragmentation fractions and mean charged track multiplicities are estimated by varying the input values of the Monte Carlo simulation by the experimental errors of the corresponding measurements or world averages. For the fragmentation fractions of c and b quarks to hadrons and for the lifetimes of these hadrons the central values and errors on the world averages are taken from [32]. For the mean charged track multiplicities the values and uncertainties for c hadrons are taken from Mark-III [33] and for b hadrons from LEP and SLD measurements [34].
- The uncertainty of the jet energy scale of 2% leads to cross section uncertainties between 3% at small p_t^{jet} and 12% at large p_t^{jet} and 6% on average, independently of the quark flavour.
- The trigger efficiency is studied using monitoring events from neutral current processes in deep inelastic scattering in which the scattered positron triggers the events independently of the triggers under study. The uncertainty is determined to be 5%.
- The luminosity is known to an accuracy of 1.5%.

Total systematic uncertainties of 14% and 22% are obtained for the measurement of the charm and the beauty production cross sections respectively. The total system-

Table 1. Systematic uncertainties of the measured total charm and beauty dijet cross sections

Source	Variation	Uncertainty [%]	
		Charm	Beauty
Impact parameter resolution	$\oplus 25\ \mu\text{m}$ $\oplus 200\ \mu\text{m}$	7	10
Jet axis ϕ direction	1° shift in ϕ	3	2
Track finding efficiency	$2\% \oplus 1\%$	3	8
uds asymmetry	$\pm 50\%$	1	6
HQ production model (PYTHIA)	resolved γ , p_t dependence	7	14
Fragmentation model	Peterson / Lund	1	2
Fragmentation fractions	PDG	0.5	1.6
Hadron lifetimes	PDG	0.1	0.3
Charged track multiplicities	MARK-III, LEP, SLD	1.5	4
Jet energy scale	2%	6	5
Trigger efficiency		5	5
Luminosity measurement		1.5	1.5
Total		14	22

atic error for the flavour inclusive dijet cross section is 8% resulting from the uncertainty of the hadronic energy scale (6%), the trigger efficiency uncertainty (5%) and the uncertainty of the luminosity measurement (1.5%). For the relative contributions of charm and beauty production to the flavour inclusive dijet cross section, the statistical errors are added in quadrature and the systematic errors include those sources that are specific to the charm and beauty cross section measurement. The same uncertainties are equally attributed to all bins of the measurement except for the uncertainty of the hadronic energy scale for which the uncertainties are determined and applied individually in each bin of the measurement.

6.2 Results

The total dijet charm photoproduction cross section in the range $Q^2 < 1 \text{ GeV}^2$, $0.15 < y < 0.8$, $p_t^{\text{jet}_{1(2)}} > 11$ (8) GeV and $-0.9 < \eta^{\text{jet}_{1(2)}} < 1.3$ is measured to be

$$\sigma(ep \rightarrow ec\bar{c}X \rightarrow ejjX) = 702 \pm 67(\text{stat.}) \pm 95(\text{syst.}) \text{ pb.}$$

For the same kinematic range, the measured beauty cross section is

$$\sigma(ep \rightarrow ebb\bar{b}X \rightarrow ejjX) = 150 \pm 17(\text{stat.}) \pm 33(\text{syst.}) \text{ pb.}$$

The predictions from the theoretical calculations are detailed in Table 2. The NLO parton level calculations are corrected to the hadron level using correction factors as determined from PYTHIA (see Sect. 5). For charm, the NLO QCD calculation FMNR is in reasonable agreement within the theoretical errors. For beauty, FMNR is lower than the data by a factor 1.8, corresponding to 1.6 standard deviations, taking both experimental uncertainties and uncertainties in the theory into account. For both, charm and beauty, PYTHIA and CASCADE predict a normalisation which is similar to that of FMNR.

The measured differential cross sections as functions of $p_t^{\text{jet}_1}$, of η and of x_γ^{obs} , are shown in Fig. 3 and listed in Table 3. PYTHIA is used to determine the point in the bin at which the bin-averaged cross section equals the differential cross section. Both the charm and beauty data are reasonably well described in shape. Towards small values

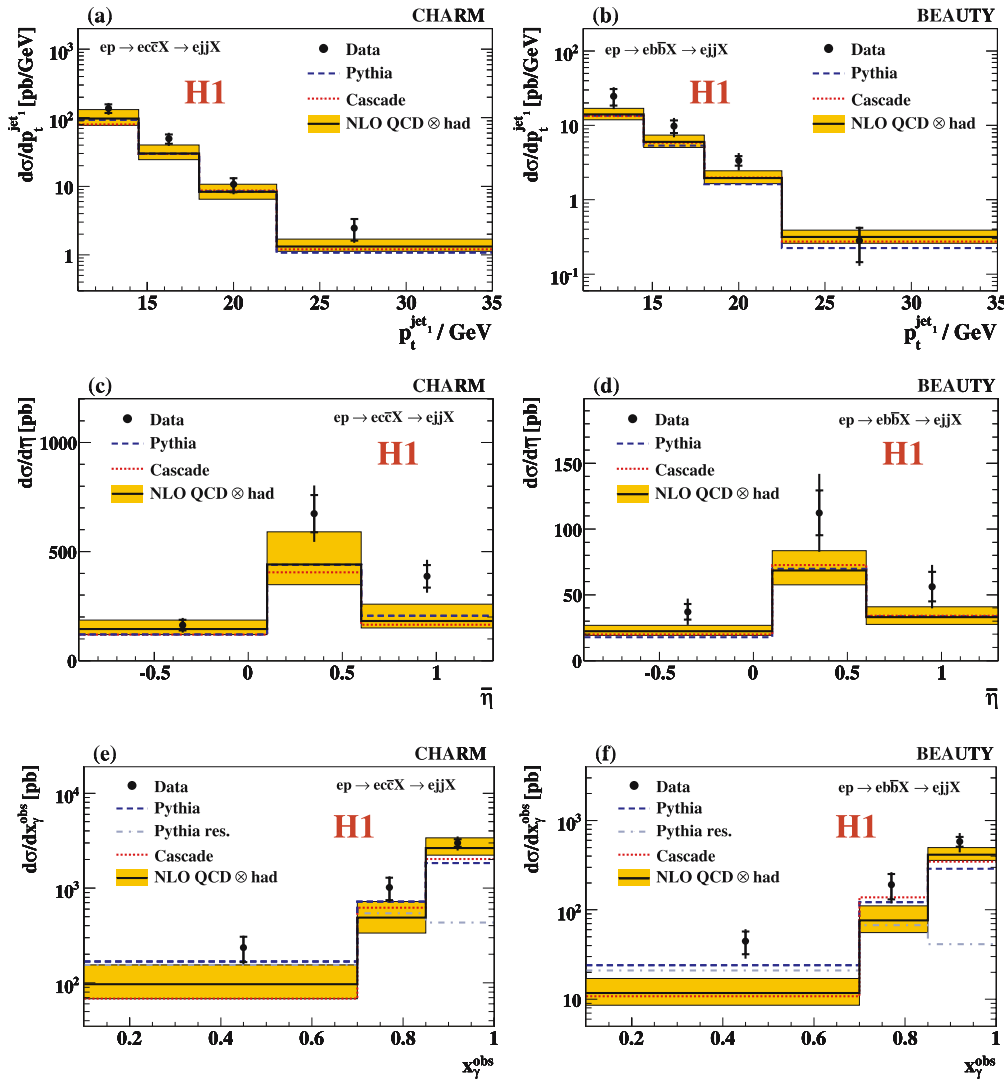


Fig. 3. Differential charm and beauty photoproduction cross sections **a,b** $d\sigma/dp_t^{\text{jet}_1}$, **c,d** $d\sigma/d\eta$ and **e,f** $d\sigma/dx_\gamma^{\text{obs}}$ for the process $ep \rightarrow e(c\bar{c} \text{ or } b\bar{b})X \rightarrow ejjX$. The *inner* error bars indicate the statistical uncertainty and the *outer* error bars show the statistical and systematic errors added in quadrature. The *solid lines* indicate the prediction from a NLO QCD calculation, corrected for hadronisation effects, and the *shaded band* shows the estimated uncertainty. The absolute predictions from PYTHIA (*dashed lines*) and CASCADE (*dotted lines*) are also shown. The contribution from resolved processes in PYTHIA (*dash-dotted lines*) is depicted separately

of x_γ^{obs} (Fig. 3f) the prediction tends to be below the data ($\sim 2\sigma$ in the lowest bin). In this region, PYTHIA predicts a large contribution from events with resolved photons, as indicated in the figures by the dashed-dotted lines.

PYTHIA describes the shapes of the charm and beauty data distributions, while the normalisations are low. The CASCADE prediction is too small in the region of small x_γ^{obs} , but approaches the measurement in the region $x_\gamma^{\text{obs}} > 0.85$.

Table 2. The measured charm and beauty photoproduction dijet cross sections in the kinematic range $Q^2 < 1 \text{ GeV}^2$, $0.15 < y < 0.8$, $p_t^{\text{jet}_{1(2)}} > 11$ (8) GeV and $-0.9 < \eta^{\text{jet}_{1(2)}} < 1.3$ in comparison to predictions in NLO QCD (FMNR) and from the Monte Carlo programs PYTHIA and CASCADE

	Charm [pb]	Beauty [pb]
Data	$702 \pm 67(\text{stat.}) \pm 95(\text{syst.})$	$150 \pm 17(\text{stat.}) \pm 33(\text{syst.})$
FMNR	500^{+173}_{-99}	83^{+19}_{-14}
PYTHIA	484	76
CASCADE	438	80

Table 3. The measured charm and beauty dijet photoproduction cross sections and the relative contributions $f^{c\bar{c}}$ and $f^{b\bar{b}}$ to the inclusive dijet photoproduction cross section with statistical and systematic errors

Charm								
$p_t^{\text{jet}_1}$ range [GeV]	$\langle p_t^{\text{jet}_1} \rangle$ [GeV]	$d\sigma/dp_t^{\text{jet}_1}$ [pb/GeV]	stat.	syst.	$f^{c\bar{c}}$	stat.	syst.	
11.0	14.5	12.75	137	20	20	0.333	0.048	0.044
14.5	18.0	16.25	49.5	7.6	7.9	0.352	0.054	0.046
18.0	22.5	20.0	10.6	2.5	1.8	0.270	0.062	0.035
22.5	35.0	27.0	2.46	0.86	0.45	0.402	0.140	0.052
$\bar{\eta}$ range	$\langle \bar{\eta} \rangle$	$d\sigma/d\bar{\eta}$ [pb]	stat.	syst.	$f^{c\bar{c}}$	stat.	syst.	
-0.90	0.10	-0.35	162	24	22	0.337	0.051	0.045
0.10	0.60	0.35	674	86	101	0.346	0.044	0.045
0.60	1.30	0.95	386	52	61	0.358	0.049	0.047
x_γ^{obs} range	$\langle x_\gamma^{\text{obs}} \rangle$	$d\sigma/dx_\gamma^{\text{obs}}$ [pb]	stat.	syst.	$f^{c\bar{c}}$	stat.	syst.	
0.10	0.70	0.45	236	70	34	0.250	0.074	0.033
0.70	0.85	0.77	1017	271	162	0.342	0.091	0.047
0.85	1.00	0.92	2994	280	498	0.374	0.035	0.049
Beauty								
$p_t^{\text{jet}_1}$ range [GeV]	$\langle p_t^{\text{jet}_1} \rangle$ [GeV]	$d\sigma/dp_t^{\text{jet}_1}$ [pb/GeV]	stat.	syst.	$f^{b\bar{b}}$	stat.	syst.	
11.0	14.5	12.75	24.7	6.1	5.5	0.060	0.015	0.013
14.5	18.0	16.25	9.79	1.87	2.15	0.070	0.013	0.015
18.0	22.5	20.0	3.37	0.48	0.78	0.085	0.012	0.018
22.5	35.0	27.0	0.28	0.14	0.07	0.046	0.022	0.010
$\bar{\eta}$ range	$\langle \bar{\eta} \rangle$	$d\sigma/d\bar{\eta}$ [pb]	stat.	syst.	$f^{b\bar{b}}$	stat.	syst.	
-0.90	0.10	-0.35	37.1	5.9	7.8	0.077	0.012	0.016
0.10	0.60	0.35	112	17	25	0.057	0.009	0.012
0.60	1.30	0.95	56.2	11.3	12.4	0.052	0.010	0.011
x_γ^{obs} range	$\langle x_\gamma^{\text{obs}} \rangle$	$d\sigma/dx_\gamma^{\text{obs}}$ [pb]	stat.	syst.	$f^{b\bar{b}}$	stat.	syst.	
0.10	0.70	0.45	44.6	12.8	9.9	0.047	0.014	0.010
0.70	0.85	0.77	191	60	44	0.064	0.020	0.014
0.85	1.00	0.92	584	72	135	0.073	0.009	0.015

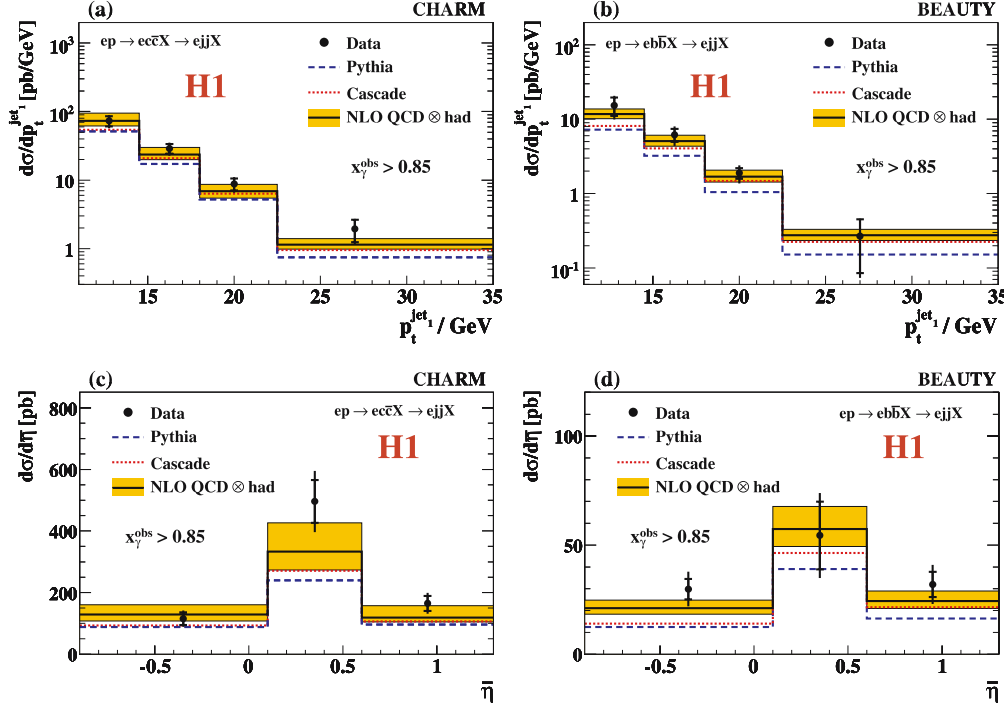


Fig. 4. Differential charm and beauty photoproduction cross sections **a,b** $d\sigma/dp_t^{\text{jet}1}$ and **c,d** $d\sigma/d\bar{\eta}$ for the process $ep \rightarrow e(c\bar{c} \text{ or } b\bar{b})X \rightarrow ejjX$ in the region $x_\gamma^{\text{obs}} > 0.85$. The *inner* error bars indicate the statistical uncertainty and the *outer* error bars show the statistical and systematic errors added in quadrature. The *solid lines* indicate the prediction from a NLO QCD calculation, corrected for hadronisation effects, and the *shaded band* shows the estimated uncertainty. The absolute predictions from PYTHIA (*dashed lines*) and CASCADE (*dotted lines*) are also shown

Table 4. The measured charm and beauty dijet photoproduction cross sections and the relative contributions $f^{c\bar{c}}$ and $f^{b\bar{b}}$ to the inclusive photoproduction dijet cross section for the region $x_\gamma^{\text{obs}} > 0.85$ with statistical and systematic errors

Charm									
$p_t^{\text{jet}1}$ range [GeV]		$\langle p_t^{\text{jet}1} \rangle$ [GeV]	$d\sigma/dp_t^{\text{jet}1}$ [pb/GeV]	stat.	syst.	$f^{c\bar{c}}$	stat.	syst.	
11.0	14.5	12.75	73.3	12.7	10.7	0.348	0.060	0.046	
14.5	18.0	16.25	29.0	4.6	4.6	0.364	0.057	0.048	
18.0	22.5	20.0	8.79	1.75	1.46	0.357	0.071	0.047	
22.5	35.0	27.0	1.94	0.70	0.35	0.455	0.165	0.060	
$\bar{\eta}$ range		$\langle \bar{\eta} \rangle$	$d\sigma/d\bar{\eta}$ [pb]	stat.	syst.	$f^{c\bar{c}}$	stat.	syst.	
-0.90	0.10	-0.35	115	21	16	0.322	0.058	0.043	
0.10	0.60	0.35	496	70	74	0.462	0.065	0.060	
0.60	1.30	0.95	165	24	26	0.374	0.055	0.049	
Beauty									
$p_t^{\text{jet}1}$ range [GeV]		$\langle p_t^{\text{jet}1} \rangle$ [GeV]	$d\sigma/dp_t^{\text{jet}1}$ [pb/GeV]	stat.	syst.	$f^{b\bar{b}}$	stat.	syst.	
11.0	14.5	12.75	15.3	4.3	3.4	0.073	0.020	0.015	
14.5	18.0	16.25	6.19	1.20	1.42	0.078	0.015	0.016	
18.0	22.5	20.0	1.89	0.31	0.44	0.076	0.013	0.016	
22.5	35.0	27.0	0.27	0.18	0.07	0.063	0.043	0.014	
$\bar{\eta}$ range		$\langle \bar{\eta} \rangle$	$d\sigma/d\bar{\eta}$ [pb]	stat.	syst.	$f^{b\bar{b}}$	stat.	syst.	
-0.90	0.10	-0.35	29.8	4.7	6.3	0.084	0.013	0.018	
0.10	0.60	0.35	54.4	15.5	12.0	0.051	0.014	0.011	
0.60	1.30	0.95	31.9	5.7	7.1	0.072	0.013	0.016	

Differential cross sections are also measured separately for the region $x_\gamma^{\text{obs}} > 0.85$ and the results as functions of $p_t^{\text{jet}1}$ and of $\bar{\eta}$ are shown in Fig. 4 and listed in Table 4. The charm cross sections are in good agreement with the NLO QCD calculation both in normalisation and shape. The beauty cross sections are also reasonably well described, the agreement being better than for the whole range of x_γ^{obs} .

The relative contributions from charm and beauty to the inclusive dijet cross sections are presented in Fig. 5 and listed in Tables 3 and 4. In Fig. 5a, the relative contributions are shown as a function of x_γ^{obs} . The data are compared with the PYTHIA Monte Carlo simulation which predicts an increase of the relative charm and beauty con-

tributions towards large x_γ^{obs} where direct photon–gluon fusion processes dominate.

Assuming the charm and beauty quarks to be light, naïve quark charge counting predicts a value of four for the relative production rates of charm to beauty dijets in direct photon–gluon fusion processes. In comparison, the measurement in the region $x_\gamma^{\text{obs}} > 0.85$ yields a ratio of 5.1 ± 1.1 (stat.). In Fig. 5b and c the relative contributions to the dijet cross section are shown for the region $x_\gamma^{\text{obs}} > 0.85$ as a function of $p_t^{\text{jet}1}$ and of $\bar{\eta}$. The ratios are constant within their uncertainties.

7 Heavy quark enriched data sample

In order to study the description of the data by the PYTHIA Monte Carlo further, a subsample of events is

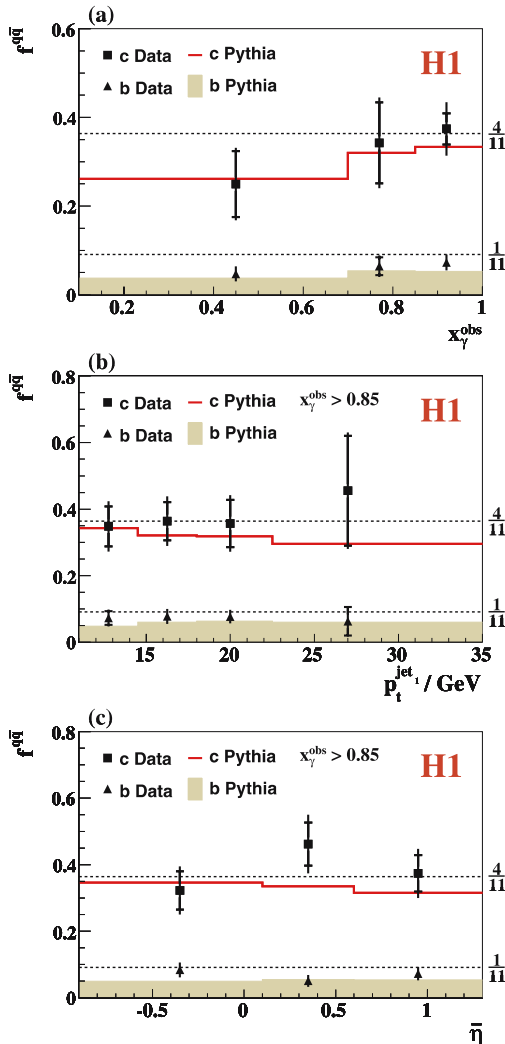


Fig. 5. Relative contributions from charm (*squares*) and beauty events (*triangles*) as a function of **a** the observable x_γ^{obs} , **b** the transverse momentum $p_t^{\text{jet}1}$ of the leading jet for $x_\gamma^{\text{obs}} > 0.85$ and **c** the mean pseudo-rapidity $\bar{\eta}$ of the two jets for $x_\gamma^{\text{obs}} > 0.85$. The *inner error bars* indicate the statistical uncertainty and the *outer error bars* show the statistical and systematic error added in quadrature. The *solid line* (*shaded area*) indicates the absolute prediction from PYTHIA for charm (beauty)

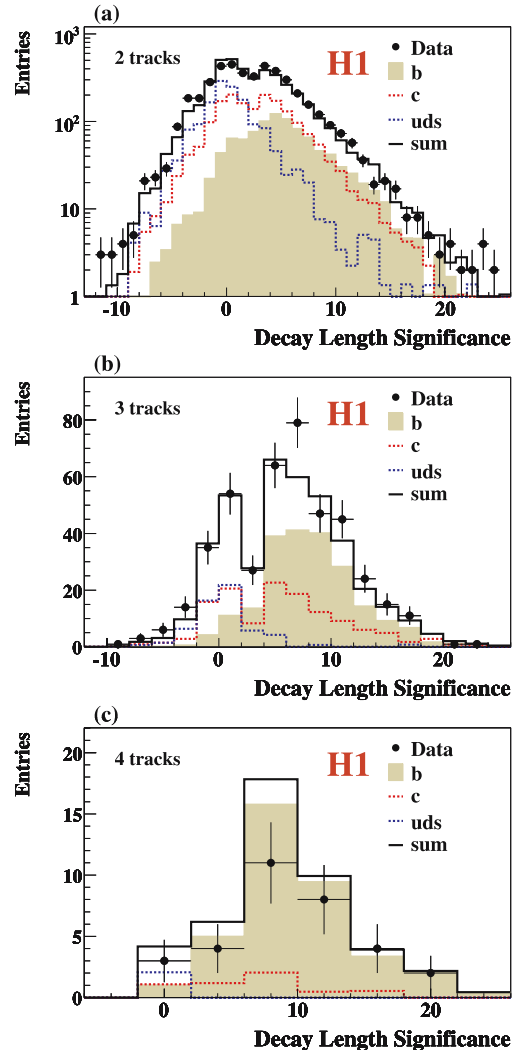


Fig. 6. Decay length significance distributions for samples of events with a secondary vertex reconstructed from **a** 2, **b** 3 and **c** 4 tracks. The data (*points*) are compared with the PYTHIA simulation after applying the scale factors as obtained from the fit to the subtracted significance distributions of the full sample

used, in which the fraction of events containing heavy quarks is enriched. For this subsample secondary vertices of the heavy hadron decays are reconstructed explicitly using events with at least two selected tracks in a given jet. The relative fraction of heavy quarks in the event sample is then further enhanced by subsequent cuts on the secondary vertex track multiplicity and the decay length significance. For this heavy quark enriched sample the distributions of the jet transverse momentum, the mean pseudo-rapidity and the observable x_γ^{obs} are presented and the decomposition and shape differences of direct and resolved photon processes, as implemented in PYTHIA, are studied.

Using a method presented in a previous H1 publication [5] the primary vertex and the secondary vertices of the heavy hadron decays are reconstructed. For each jet the associated tracks are used to reconstruct a secondary vertex in an iterative procedure. No definite assignment of tracks to vertices is made, but each track is assigned a weight in the range 0 to 1 for each vertex candidate, using the weight function of [35]. The smaller the distance of the track to the vertex candidate, the larger the weight.

For each jet the vertex configuration that minimises the global fit χ^2 is found iteratively using deterministic annealing [36]. The number of tracks which contribute with a weight greater than 0.8 to the secondary vertex is used as a measure of the decay vertex track multiplicity. The decay length significance is given by the transverse distance between the primary and the secondary vertex divided by its error. The sign is defined using the projection of the corresponding vector on the jet direction. Figure 6 shows the decay length significance distributions for different decay track multiplicities. Good agreement is seen between the data and the distributions from the PYTHIA Monte Carlo simulation which are scaled by the factors as obtained from the fit to the subtracted significance distributions S_1 and S_2 . Conversely, a simultaneous fit of the decay length significance distributions for the different track multiplicities gives results consistent with those from the subtracted significance distributions.

Figure 6 shows that in heavy quark events secondary vertices are significantly displaced in the direction of the related jet axis. Contributions from light quarks are

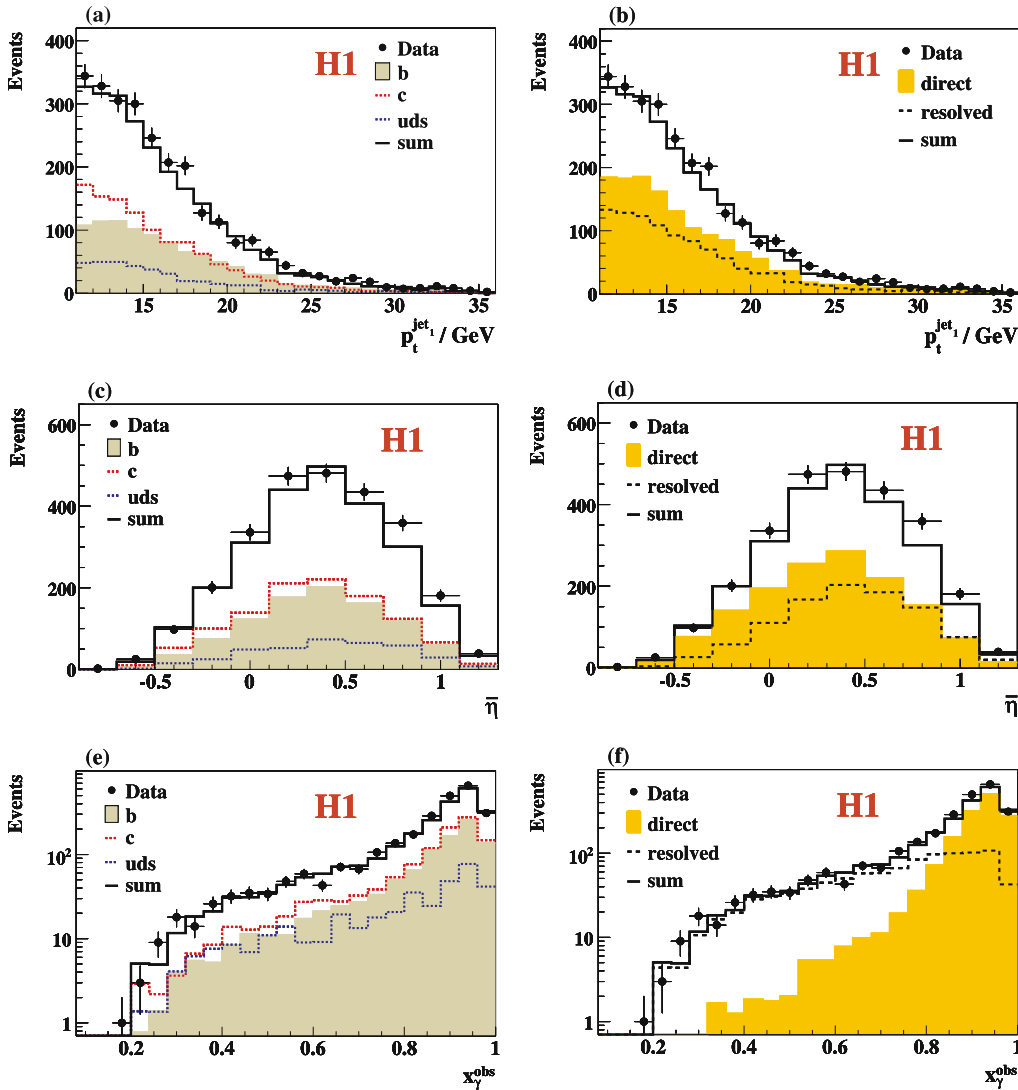


Fig. 7. Distributions of the heavy quark enriched sample with two or more tracks originating from a secondary vertex and a decay length significance larger than 2.0 (see text). The data are compared to the PYTHIA simulation for the distributions of **a,b** the transverse momentum $p_t^{\text{jet}1}$ of the leading jet, **c,d** the mean pseudo-rapidity $\bar{\eta}$ of the two jets and **e,f** the observable x_γ^{obs} . The *left column* shows the decomposition of the distribution into beauty, charm and light quarks after scaling the PYTHIA predictions by the scale factors obtained from the fit to the subtracted significance distributions of the full sample. In the *right column* the contributions from direct and resolved processes in PYTHIA are indicated as *shaded histogram* and *dashed line* respectively

mainly observed in the two-track sample at small decay length significances. In the two-track sample the contribution from charm and beauty is similar to that of light quark events while the three and four-track samples are dominated by the beauty component, as expected from the mean charged particle multiplicity in heavy hadron decays.

The fraction of events with heavy quarks is enhanced by requiring a secondary decay vertex with two or more tracks and a decay length significance larger than 2.0. Applying these cuts, the distributions for p_t^{jet1} , for $\bar{\eta}$ and for x_γ^{obs} are shown in Fig. 7. The data are compared to the PYTHIA Monte Carlo simulations. In Fig. 7a, c and e the decomposition into light, charm and beauty quark contributions is indicated. These are determined using the scale factors as obtained from the fit to the subtracted significance distributions of the full sample. Good agreement between the PYTHIA prediction and the data is seen. The contributions from charm and beauty events are 44% and 41% respectively, while 15% of the events contain only light quarks. In Fig. 7b, d and f the same data are shown together with the contributions from direct ($\gamma g \rightarrow q\bar{q}$) and resolved processes, as predicted by the PYTHIA simulation. According to the leading order QCD calculation, as implemented in PYTHIA, the fraction of events that arise from processes with resolved photons is about 40%.

In the region $x_\gamma^{\text{obs}} < 0.85$ the contribution from resolved processes is enhanced and amounts to about 80%. According to PYTHIA the contribution from processes with heavy quark excitation is dominant. In conclusion, the data are well described by the leading order Monte Carlo simulation PYTHIA in which significant contributions from heavy quark excitation processes are predicted.

8 Conclusions

Differential charm and beauty dijet photoproduction cross sections at HERA are measured using a technique based on the lifetime of the heavy quark hadrons. The heavy quark cross sections are determined using the subtracted impact parameter significance distributions of tracks in dijet events. The cross sections are measured as functions of the transverse momentum p_t^{jet1} of the leading jet, of the mean pseudo-rapidity $\bar{\eta}$ of the two jets and of the observable x_γ^{obs} . Taking into account the theoretical uncertainties, the charm cross sections are consistent both in normalisation and shape with a calculation in perturbative QCD to next-to-leading order. The beauty cross sections tend to be higher than NLO, by 1.6σ for the total cross section, with an increased difference observed in the region of $x_\gamma^{\text{obs}} < 0.85$ where processes involving resolved photons or higher order contributions are expected to be enhanced. The Monte Carlo generator PYTHIA gives a good description of the shape of both the charm and the beauty data. The data confirm the expectation within this model that a significant contribution to the heavy quark

dijet cross section comes from processes with resolved photons. In the region $x_\gamma^{\text{obs}} > 0.85$, the relative contributions from charm and beauty to the inclusive dijet cross section are found to be in agreement within errors with values of 4/11 and 1/11, i.e. the naïve expectation for the direct photon–gluon fusion process, assuming all quarks to be massless.

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